

Renwal

60581

Code - A

Subject Elementary Topology
(Reappear)

Set _____

ANSWER - KEY

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| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| 4 | 1 | 3 | 4 | 3 | 4 | 1 | 1 | 1 | 3 |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 2 | 4 | 2 | 1 | 4 | 1 | 1 | 4 | 3 | 2 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 3 | 1 | 3 | 1 | 1 | 1 | 4 | 2 | 3 | 1 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 2 | 3 | 4 | 4 | 1 | 3 | 4 | 1 | 2 | 3 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
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Revised
Code-B

Subject Elementary Topology

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ANSWER - KEY

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| 4 | 1 | 3 | 4 | 3 | 4 | 1 | 1 | 1 | 3 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 2 | 4 | 2 | 1 | 4 | 1 | 1 | 4 | 3 | 2 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 3 | 1 | 3 | 1 | 1 | 1 | 4 | 2 | 3 | 1 |
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(Signature of the Paper-Setter)

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Revised
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Subject Elementary Topology
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ANSWER - KEY

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| 1 | 1 | 2 | 4 | 1 | 1 | 1 | 2 | 1 | 3 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 4 | 1 | 3 | 4 | 3 | 4 | 1 | 1 | 1 | 3 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 2 | 4 | 2 | 1 | 4 | 1 | 1 | 4 | 3 | 2 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
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(Signature of the Paper-Setter)

60581

Code D

Pass

Subject Elementary Topology
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ANSWER - KEY

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| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 2 | 3 | 4 | 4 | 1 | 3 | 4 | 1 | 2 | 3 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 1 | 1 | 2 | 4 | 1 | 1 | 1 | 2 | 1 | 3 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 4 | 1 | 3 | 4 | 3 | 4 | 1 | 1 | 1 | 3 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 2 | 4 | 2 | 1 | 4 | 1 | 1 | 4 | 3 | 2 |

(Signature of the Paper-Setter)

1. Let X be a non-empty set. Let T_1 and T_2 be two topologies on X such that T_1 is strictly contained in T_2 . If $I : (X, T_1) \rightarrow (X, T_2)$ is identity map, then:
 - (1) both I and I^{-1} are continuous
 - (2) both I and I^{-1} are not continuous
 - (3) I is continuous but I^{-1} is not continuous
 - (4) I is not continuous but I^{-1} is continuous
2. The connected subset of real line with usual topology are --:
 - (1) all intervals
 - (2) only bounded intervals
 - (3) only compact intervals
 - (4) only semi-infinite intervals
3. Topological space X is locally path connected space-
 - (1) if X is locally connected at each $x \notin X$
 - (2) if X is locally connected at some $x \in X$
 - (3) if X is locally connected at each $x \in X$
 - (4) None of these
4. The topology on real line R generated by left-open right closed intervals $(a, b]$ is:
 - (1) strictly coarser than usual topology
 - (2) strictly finer than usual topology
 - (3) not comparable with usual topology
 - (4) same as the usual topology

5. Which of the following is not first countable?

- (1) discrete space
- (2) indiscrete space
- (3) cofinite topological space on \mathbb{R}
- (4) metric space

6. Let $X = \{a, b, c\}$ and $\mathcal{T}_1 = \{\emptyset, \{a\}, \{b, c\}, X\}$

$X^* = \{x, y, z\}$ and $\mathcal{T}_2 = \{\emptyset, \{x\}, \{y, z\}, X^*\}$

Then which of the following mapping from X to X^* are continuous?

- (1) $f(a) = x, f(b) = y, f(c) = z$
- (2) $g(a) = x, g(b) = y, g(c) = z$
- (3) $h(a) = z, h(b) = x, h(c) = y$
- (4) both (1) and (2)

7. A subspace of Hausdorff space is -

- (1) Hausdorff space
- (2) Discrete space
- (3) Closed set
- (4) None of these

8. Let X be a topological space satisfy first countability axiom if -

- (1) the point $x \in \overline{A}$, closure of $A \subset X$ iff there is a sequence of points of A converging to x
- (2) The point $x \in \overline{A}$, closure of $A \subset X$ iff there is a sequence of point of A diverging to x
- (3) The point $x \in \overline{A}$, closure of $A \subset X$ iff there is a sequence of point of A converging to zero
- (4) None of these

9. Let X be non-empty compact Hausdorff space if every point of X is limit point of X , then:
- (1) X is uncountable
 - (2) X is countable
 - (3) X is disjoint
 - (4) none of these
10. Let T_1 and T_2 be topological space. Under which condition a function $f : T_1 \rightarrow T_2$ is said to continuous?
- (1) iff pre-images of open sets are open
 - (2) iff pre images of every member of a base of T_2 is an open set in T_1
 - (3) both (1) and (2)
 - (4) iff pre-images of closed sets are not closed
11. Let $f : R \rightarrow R$ be continuous function and let S be non-empty proper subset of R . Which one of following statements is always true? (Here \bar{A} denote closure of A and A^0 denote interior of A)
- (1) $f(S)^0 \subseteq f(S^0)$
 - (2) $f(\bar{S}) \subseteq \overline{f(S)}$
 - (3) $f(\bar{S}) \supseteq \overline{f(S)}$
 - (4) $f(S)^0 \supseteq f(S^0)$
12. Let $T_1 = \{G \subseteq R : G \text{ is finite or } R/G \text{ is finite}\}$ and $T_2 = \{G \subseteq R : G \text{ is countable or } R/G \text{ is countable}\}$ then -
- (1) neither T_1 or T_2 is topology on R
 - (2) T_1 is topology on R but T_2 is not topology on R
 - (3) T_2 is topology on R but T_1 is not topology on R
 - (4) Both T_1 and T_2 are topologies on R

13. Let (X,T) be topological space. Every component of (X,T) is -
- (1) open
 - (2) closed
 - (3) both (1) and (2)
 - (4) none of these
14. Which of the following space is T_0 -space, T_1 -space and T_2 -space?
- (1) discrete space
 - (2) indiscrete space
 - (3) co-finite topological space
 - (4) both (1) and (2)
15. A finite space with cofinite topology is-
- (1) separable
 - (2) first-countable
 - (3) second-countable
 - (4) All of above
16. A sub-basis T for topology X is collection of subsets of X -
- (1) whose union equals X
 - (2) whose union is subset of X
 - (3) whose union is superset of X
 - (4) none of these
17. Every closed interval of real line R is -
- (1) uncountable
 - (2) countable
 - (3) disjoint
 - (4) none of these

18. Which of the following is not true?

- (1) if $A \subseteq B$ and $A^0 \subseteq B^0$
- (2) every limit point is an adherent point
- (3) $(A \cap B)^0 = A^0 \cap B^0$
- (4) $(A \cup B)^0 \subseteq A^0 \cup B^0$

19. If Y is subspace of X . If A is closed in Y and Y is closed in X , then-

- (1) A is semi-closed in X
- (2) A is open in X
- (3) A is closed in X
- (4) none of these

20. If T_1 and T_2 are two topologies on non-empty set X , then which of the following is a topological space-

- (1) $T_1 \cup T_2$
- (2) $T_1 \cap T_2$
- (3) T_1 / T_2
- (4) none of these

21. Which of the following statement is true about lower limit topology on \mathbb{R} ?

- (1) it is first countable
- (2) it is not separable
- (3) it is second countable
- (4) none of above

22. If X is topological space, then-

- (1) each path component of X lies in component of X
- (2) some path component of X lies in component of X
- (3) each path component of X does not lie in component of X
- (4) none of these

23. Let $X = \{a, b, c\}$ and $T = \{\emptyset, \{a\}, \{b, c\}, X\}$ which of the following is true?
- (1) $d(\{A\}) = \{B\}$
 - (2) $d(\{c\}) = \{a\}$
 - (3) $d(\{b, c\}) = \{b, c\}$
 - (4) $d(\{a, c\}) = \{c\}$
24. Let (X, T) is given topological space, $A \subset X$, then closure of A -
- (1) is the intersection of all closed sets containing A
 - (2) is the union of all closed sets containing A
 - (3) is the intersection of all open sets containing A
 - (4) none of these
25. If Y is subspace of X , $A \subset Y$ and \bar{A} is closure of A in X then closure of A in Y -
- (1) is equal to $A \cap Y$
 - (2) is equal to $A \cup Y$
 - (3) is equal to Y
 - (4) none of these
26. Suppose $X = \{\alpha, \beta, \delta\}$ and
 let $T_1 = \{\emptyset, X, \{\alpha\}, \{\alpha, \beta\}\}$ and
 $T_2 = \{\emptyset, X, \{\alpha\}, \{\beta, \delta\}\}$
 then -
- (1) both $T_1 \cap T_2$ and $T_1 \cup T_2$ are topologies
 - (2) neither $T_1 \cap T_2$ nor $T_1 \cup T_2$ is topology
 - (3) $T_1 \cup T_2$ is topology but $T_1 \cap T_2$ is not a topology
 - (4) $T_1 \cap T_2$ is topology but $T_1 \cup T_2$ is not topology

27. Let E be connected subset of \mathbb{R} with atleast two elements. Then number of elements in E is-
- (1) exactly two
 - (2) more than two but finite
 - (3) countably infinite
 - (4) uncountable
28. Let T be topology on non-empty set X . Under which condition topological space (X, T) is connected-
- (1) iff these exists no non-empty subsets of X which are both open and closed
 - (2) iff these exists no non-empty proper subset of X which are both open and closed
 - (3) iff these exists non-empty proper subsets of X which are both open and closed
 - (4) iff these exists non-empty subsets of X which are both open and closed
29. Let X, Y be topological space and $f : X \rightarrow Y$ be continuous and bijective map. Then f is homomorphism if:
- (1) X and Y are compact
 - (2) X is Hausdorff and Y is compact
 - (3) X is compact and Y is Hausdorff
 - (4) X and Y are Hausdorff
30. Under which condition a finite topological space is T_1 -space?
- (1) iff it is discrete
 - (2) iff it is indiscrete
 - (3) both (1) and (2)
 - (4) none of these

31. Every closed subspace of Lindelöf space is-
- (1) closed
 - (2) Lindelöf
 - (3) both (1) and (2)
 - (4) none of these
32. Let X be first countable space. Every convergent sequence has a unique limit point iff-
- (1) it is T_1 -space
 - (2) it is T_0 -space
 - (3) it is T_2 -space
 - (4) none of these
33. In which space, no finite set has a limit point?
- (1) T_0 -space
 - (2) T_2 -space
 - (3) Lindelöf space
 - (4) T_1 -space
34. Which of the following statement is true?
- P : Every T_1 -space is T_0 -space
- Q : Every first - countable is second - countable
- R : Every T_0 -space is T_1 -space
- S : Every second-countable is first-countable
- (1) P and Q
 - (2) Q and R
 - (3) R and S
 - (4) P and S

35. A subset Y of a topological space X is dense in X if
- (1) $\bar{Y} = X$
 - (2) $Y = X$
 - (3) $\bar{Y} \not\subseteq X$
 - (4) none of these
36. Which of the following space is T_0 -space, T_1 -space and T_2 -space?
- (1) indiscrete space
 - (2) co-finite topological space
 - (3) discrete space
 - (4) both (1) and (2)
37. Which of the following space is not connected?
- (1) $\{\phi, \{a\}, X\}$ where $X = \{a, b\}$
 - (2) infinite cofinite topological space
 - (3) indiscrete space
 - (4) discrete space with more than one point
38. Let A, B be subsets of topological space (X, T) , then which of the following is true?
- (1) $d(A \cup B) = d(A) \cup d(B)$
 - (2) $d(A \cup B) \neq d(A) \cup d(B)$
 - (3) $d(A \cap B) = d(A) \cap d(B)$
 - (4) $d(A \cap B) \supseteq d(A) \cap d(B)$

39. A countable product of first countable spaces is:
- (1) second - countable
 - (2) first - countable
 - (3) not first - countable
 - (4) third countable
40. Every Hausdorff topological space is:
- (1) normal
 - (2) regular
 - (3) completely regular
 - (4) none of these
41. Consider topology T_1 is the topology generated by all unions of intervals of form-
- $$\{(a,b) : a, b \in \mathbb{R}, a \leq b\}$$
- and T_2 is discrete topology
- Then which of the following is true?
- (1) T_1 is strictly coarser than T_2
 - (2) T_1 is finer than T_2
 - (3) T_2 is finer than T_1
 - (4) T_1 is coarser than T_2
42. A topological space X is compact if open covering of X contains-
- (1) finite subcollection that covers X
 - (2) infinite subcollection that covers X
 - (3) finite subcollection that does not cover X
 - (4) none of these

43. Consider \mathbb{R}^2 with usual topology. Let

$$S = \{(x, y) \in \mathbb{R}^2 : x \text{ is an integer}\}$$

Then S is :

- (1) open but not closed
- (2) both open and closed
- (3) neither open nor closed
- (4) closed but not open

44. Suppose (X, T) is topological space. Let $\{S_n\}_{n \geq 1}$ be sequence of subsets of X.

Then-

- (1) $(S_1 \cup S_2)^0 = S_1^0 \cup S_2^0$
- (2) $(\bigcup_n S_n)^0 = \bigcup_n S_n^0$
- (3) $\overline{\bigcup_n S_n} = \bigcup_n \overline{S_n}$
- (4) $\overline{S_1 \cup S_2} = \overline{S_1} \cup \overline{S_2}$

45. A subspace of first countable space is-

- (1) first countable
- (2) not first-countable
- (3) second - countable
- (4) none of these

46. Let X and Y be topological spaces. A map $f : X \rightarrow Y$ is closed map if :

- (1) for every closed set U of X, the set $f(U)$ is closed in Y
- (2) for every open set U of X, the set $f(U)$ is closed in Y
- (3) for every closed set U of X, the set $f(U)$ is open in Y
- (4) none of these

47. Let β and β' be basis for topologies T and T' respectively on X . Then T' is finer than T is equivalent to -
- (1) for each $x \in X$ and each basis element $B \in \beta$ containing x , there is basis element $B' \in \beta'$ such that $x \in B' \subset B$
 - (2) for some $x \in X$ and each basis element $B \in \beta$ containing x , there is a basis element $B' \in \beta'$ such that $x \in B' \subset B$
 - (3) for $x \in X$ and basis element $B \in \beta$ containing x , there is basis element $B' \in \beta'$ such that $x \in B' \subset B$
 - (4) none of these
48. A collection G of subsets of topological space satisfies finite intersection condition if for every finite subcollection $\{C_1, C_2, \dots, C_n\}$ of G , the intersection -
- (1) is null set
 - (2) is not null set
 - (3) is set G
 - (4) none of these
49. The product of two Hausdorff space is-
- (1) Hausdorff space
 - (2) discrete space
 - (3) closed set
 - (4) none of these
50. Let X and Y be topological spaces. Function f is homomorphism if :
- (1) function $f : X \rightarrow Y$ is one to one function
 - (2) function f is continuous
 - (3) inverse function $f^{-1} : Y \rightarrow X$ is continuous
 - (4) all of the above

1. Consider topology T_1 is the topology generated by all unions of intervals of form-

$$\{(a,b) : a, b \in \mathbb{R}, a \leq b\}$$

and T_2 is discrete topology

Then which of the following is true?

- (1) T_1 is strictly coarser than T_2
 (2) T_1 is finer than T_2
 (3) T_2 is finer than T_1
 (4) T_1 is coarser than T_2
2. A topological space X is compact if open covering of X contains-
- (1) finite subcollection that covers X
 (2) infinite subcollection that covers X
 (3) finite subcollection that does not cover X
 (4) none of these
3. Consider \mathbb{R}^2 with usual topology. Let

$$S = \{(x,y) \in \mathbb{R}^2 : x \text{ is an integer}\}$$

Then S is :

- (1) open but not closed
 (2) both open and closed
 (3) neither open nor closed
 (4) closed but not open
4. Suppose (X,T) is topological space. Let $\{S_n\}_{n \geq 1}$ be sequence of subsets of X . Then-

(1) $(S_1 \cup S_2)^0 = S_1^0 \cup S_2^0$

(2) $(\bigcup_n S_n)^0 = \bigcup_n S_n^0$

(3) $\overline{\bigcup_n S_n} = \bigcup_n \overline{S_n}$

(4) $\overline{S_1 \cup S_2} = \overline{S_1} \cup \overline{S_2}$

5. A subspace of first countable space is-
- (1) first countable
 - (2) not first-countable
 - (3) second - countable
 - (4) none of these
6. Let X and Y be topological spaces. A map $f : X \rightarrow Y$ is closed map if :
- (1) for every closed set U of X , the set $f(U)$ is closed in Y
 - (2) for every open set U of X , the set $f(U)$ is closed in Y
 - (3) for every closed set U of X , the set $f(U)$ is open in Y
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7. Let β and β' be basis for topologies T and T' respectively on X . Then T' is finer than T is equivalent to -
- (1) for each $x \in X$ and each basis element $B \in \beta$ containing x , there is basis element $B' \in \beta'$ such that $x \in B' \subset B$
 - (2) for some $x \in X$ and each basis element $B \in \beta$ containing x , there is a basis element $B' \in \beta'$ such that $x \in B' \subset B$
 - (3) for $x \in X$ and basis element $B \in \beta$ containing x , there is basis element $B' \in \beta'$ such that $x \in B' \subset B$
 - (4) none of these
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- (1) is null set
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 - (3) is set G
 - (4) none of these

9. The product of two Hausdorff space is-
- (1) Housdorff space
 - (2) discrete space
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 - (4) none of these
10. Let X and Y be topological spaces. Function f is homomorphism if :
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 - (2) if X is locally connected at some $x \in X$
 - (3) if X is locally connected at each $x \in X$
 - (4) None of these

14. The topology on real line \mathbb{R} generated by left-open right closed intervals (a,b) is:
- (1) strictly coarser than usual topology
 - (2) strictly finer than usual topology
 - (3) not comparable with usual topology
 - (4) same as the usual topology
15. Which of the following is not first countable?
- (1) discrete space
 - (2) indiscrete space
 - (3) cofinite topological space on \mathbb{R}
 - (4) metric space
16. Let $X = \{a,b,c\}$ and $\mathcal{T}_1 = \{\emptyset, \{a\}, \{b,c\}, X\}$
 $X^* = \{x, y, z\}$ and $\mathcal{T}_2 = \{\emptyset, \{x\}, \{y,z\}, X^*\}$
- Then which of the following mapping from X to X^* are continuous?
- (1) $f(a) = x, f(b) = y, f(c) = z$
 - (2) $g(a) = x, g(b) = y, g(c) = z$
 - (3) $h(a) = z, h(b) = x, h(c) = y$
 - (4) both (1) and (2)
17. A subspace of Hausdorff space is -
- (1) Hausdorff space
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 - (3) Closed set
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18. Let X be a topological space satisfy first countability aniom if -
- (1) the point $x \in \overline{A}$, closure of A in X iff there is a sequence of points of A converging to x
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21. Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be continuous function and let S be non-empty proper subset of \mathbb{R} . Which one of following statements is always true? (Here \overline{A} denote closure of A and A° denote interior of A)
- (1) $f(S)^\circ \subseteq f(S^\circ)$
 - (2) $f(\overline{S}) \subseteq \overline{f(S)}$
 - (3) $f(\overline{S}) \supseteq \overline{f(S)}$
 - (4) $f(S)^\circ \supseteq f(S^\circ)$

22. Let $T_1 = \{G \subseteq \mathbb{R} : G \text{ is finite or } \mathbb{R}/G \text{ is finite}\}$ and $T_2 = \{G \subseteq \mathbb{R} : G \text{ is countable or } \mathbb{R}/G \text{ is countable}\}$ then -
- (1) neither T_1 or T_2 is topology on \mathbb{R}
 - (2) T_1 is topology on \mathbb{R} but T_2 is not topology on \mathbb{R}
 - (3) T_2 is topology on \mathbb{R} but T_1 is not topology on \mathbb{R}
 - (4) Both T_1 and T_2 are topologies on \mathbb{R}
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 - (3) whose union is superset of X
 - (4) none of these

27. Every closed interval of real line \mathbb{R} is -
- (1) uncountable
 - (2) countable
 - (3) disjoint
 - (4) none of these
28. Which of the following is not true?
- (1) if $A \subseteq B$ and $A^0 \subseteq B^0$
 - (2) every limit point is an adherent point
 - (3) $(A \cap B)^0 = A^0 \cap B^0$
 - (4) $(A \cup B)^0 \subseteq A^0 \cup B^0$
29. If Y is subspace of X . If A is closed in Y and Y is closed in X , then-
- (1) A is semi-closed in X
 - (2) A is open in X
 - (3) A is closed in X
 - (4) none of these
30. If T_1 and T_2 are two topologies on non-empty set X , then which of the following is a topological space-
- (1) $T_1 \cup T_2$
 - (2) $T_1 \cap T_2$
 - (3) T_1 / T_2
 - (4) none of these
31. Which of the following statement is true about lower limit topology on \mathbb{R} ?
- (1) it is first countable
 - (2) it is not separable
 - (3) it is second countable
 - (4) none of above

32. If X is topological space, then-

- (1) each path component of X lies in component of X
- (2) some path component of X lies in component of X
- (3) each path component of X does not lie in component of X
- (4) none of these

33. Let $X = \{a, b, c\}$ and $T = \{\emptyset, \{a\}, \{b, c\}, X\}$ which of the following is true?

- (1) $d(\{A\}) = \{B\}$
- (2) $d(\{c\}) = \{a\}$
- (3) $d(\{b, c\}) = \{b, c\}$
- (4) $d(\{a, c\}) = \{c\}$

34. Let (X, T) is given topological space, $A \subset X$, then closure of A -

- (1) is the intersection of all closed sets containing A
- (2) is the union of all closed sets containing A
- (3) is the intersection of all open sets containing A
- (4) none of these

35. If Y is subspace of X , $A \subset Y$ and \bar{A} is closure of A in X then closure of A in Y -

- (1) is equal to $A \cap Y$
- (2) is equal to $A \cup Y$
- (3) is equal to Y
- (4) none of these

36. Suppose $X = \{\alpha, \beta, \delta\}$ and

let $T_1 = \{\phi, X, \{\alpha\}, \{\alpha, \beta\}\}$ and

$T_2 = \{\phi, X, \{\alpha\}, \{\beta, \delta\}\}$

then -

- (1) both $T_1 \cap T_2$ and $T_1 \cup T_2$ are topologies
- (2) neither $T_1 \cap T_2$ nor $T_1 \cup T_2$ is topology
- (3) $T_1 \cup T_2$ is topology but $T_1 \cap T_2$ is not a topology
- (4) $T_1 \cap T_2$ is topology but $T_1 \cup T_2$ is not topology

37. Let E be connected subset of \mathbb{R} with atleast two elements. Then number of elements in E is-

- (1) exactly two
- (2) more than two but finite
- (3) countably infinite
- (4) uncountable

38. Let T be topology on non-empty set X . Under which condition topological space (X, T) is connected-

- (1) iff there exists no non-empty subsets of X which are both open and closed
- (2) iff there exists no non-empty proper subset of X which are both open and closed
- (3) iff there exists non-empty proper subsets of X which are both open and closed
- (4) iff there exists non-empty subsets of X which are both open and closed

39. Let X, Y be topological space and $f : X \rightarrow Y$ be continuous and bijective map. Then f is homomorphism if:

- (1) X and Y are compact
- (2) X is Hausdorff and Y is compact
- (3) X is compact and Y is Hausdorff
- (4) X and Y are Hausdorff

40. Under which condition a finite topological space is T_1 -space?
- (1) iff it is discrete
 - (2) iff it is indiscrete
 - (3) both (1) and (2)
 - (4) none of these
41. Every closed subspace of lindelof space is-
- (1) closed
 - (2) lindelof
 - (3) both (1) and (2)
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42. Let X be first countable space. Every convergent sequence has a unique limit point iff-
- (1) it is T_1 -space
 - (2) it is T_0 -space
 - (3) it is T_2 -space
 - (4) none of these
43. In which space, no finite set has a limit point?
- (1) T_0 -space
 - (2) T_2 -space
 - (3) lindelof space
 - (4) T_1 -space

44. Which of the following statement is true?

P : Every T_1 -space is T_0 -space

Q : Every first - countable is second - countable

R : Every T_0 -space is T_1 -space

S : Every second-countable is first-countable

(1) P and Q

(2) Q and R

(3) R and S

(4) P and S

45. A subset Y of a topological space X is dense in X if

(1) $\bar{Y} = X$

(2) $Y=X$

(3) $\bar{Y} \not\subseteq X$

(4) none of these

46. Which of the following space is T_0 -space, T_1 -space and T_2 -space?

(1) indiscrete space

(2) co-finite topological space

(3) discrete space

(4) both (1) and (2)

47. Which of the following space is not connected?

- (1) $\{\phi, \{a\}, X\}$ where $X = \{a,b\}$
- (2) infinite cofinite topological space
- (3) indiscrete space
- (4) discrete space with more than one point

48. Let A, B be subsets of topological space (X,T) , then which of the following is true?

- (1) $d(A \cup B) = d(A) \cup d(B)$
- (2) $d(A \cup B) \neq d(A) \cup d(B)$
- (3) $d(A \cap B) = d(A) \cap d(B)$
- (4) $d(A \cap B) \supseteq d(A) \cap d(B)$

49. A countable product of first countable spaces is:

- (1) second - countable
- (2) first - countable
- (3) not first - countable
- (4) third countable

50. Every Hausdorff topological space is:

- (1) normal
- (2) regular
- (3) completely regular
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 - (1) P and Q
 - (2) Q and R
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5. A subset Y of a topological space X is dense in X if
- (1) $\bar{Y} = X$
 - (2) $Y = X$
 - (3) $\bar{Y} \neq X$
 - (4) none of these
6. Which of the following space is T_0 -space, T_1 -space and T_2 -space?
- (1) indiscrete space
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7. Which of the following space is not connected?
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8. Let A, B be subsets of topological space (X, T) , then which of the following is true?
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 - (3) $d(A \cap B) = d(A) \cap d(B)$
 - (4) $d(A \cap B) \supseteq d(A) \cap d(B)$

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11. Consider topology T_1 is the topology generated by all unions of intervals of form-
 $\{(a,b) : a, b \in \mathbb{R}, a \leq b\}$
and T_2 is discrete topology
Then which of the following is true?
- (1) T_1 is strictly coarser than T_2
 - (2) T_1 is finer than T_2
 - (3) T_2 is finer than T_1
 - (4) T_1 is coarser than T_2
12. A topological space X is compact if open covering of X contains-
- (1) finite subcollection that covers X
 - (2) infinite subcollection that covers X
 - (3) finite subcollection that does not cover X
 - (4) none of these

13. Consider \mathbb{R}^2 with usual topology. Let

$$S = \{(x, y) \in \mathbb{R}^2 : x \text{ is an integer}\}$$

Then S is :

- (1) open but not closed
- (2) both open and closed
- (3) neither open nor closed
- (4) closed but not open

14. Suppose (X, T) is topological space. Let $\{S_n\}_{n \geq 1}$ be sequence of subsets of X.

Then-

- (1) $(S_1 \cup S_2)^0 = S_1^0 \cup S_2^0$
- (2) $(\bigcup_n S_n)^0 = \bigcup_n S_n^0$
- (3) $\overline{\bigcup_n S_n} = \bigcup_n \overline{S_n}$
- (4) $\overline{S_1 \cup S_2} = \overline{S_1} \cup \overline{S_2}$

15. A subspace of first countable space is-

- (1) first countable
- (2) not first-countable
- (3) second - countable
- (4) none of these

16. Let X and Y be topological spaces. A map $f : X \rightarrow Y$ is closed map if :

- (1) for every closed set U of X, the set $f(U)$ is closed in Y
- (2) for every open set U of X, the set $f(U)$ is closed in Y
- (3) for every closed set U of X, the set $f(U)$ is open in Y
- (4) none of these

17. Let β and β' be basis for topologies T and T' respectively on X . Then T' is finer than T is equivalent to -
- (1) for each $x \in X$ and each basis element $B \in \beta$ containing x , there is basis element $B' \in \beta'$ such that $x \in B' \subset B$
 - (2) for some $x \in X$ and each basis element $B \in \beta$ containing x , there is a basis element $B' \in \beta'$ such that $x \in B' \subset B$
 - (3) for $x \in X$ and basis element $B \in \beta$ containing x , there is basis element $B' \in \beta'$ such that $x \in B' \subset B$
 - (4) none of these
18. A collection G of subsets of topological space satisfies finite intersection condition if for every finite subcollection $\{C_1, C_2, \dots, C_n\}$ of G , the intersection -
- (1) is null set
 - (2) is not null set
 - (3) is set G
 - (4) none of these
19. The product of two Hausdorff space is-
- (1) Hausdorff space
 - (2) discrete space
 - (3) closed set
 - (4) none of these
20. Let X and Y be topological spaces. Function f is homomorphism if :
- (1) function $f : X \rightarrow Y$ is one to one function
 - (2) function f is continuous
 - (3) inverse function $f^{-1} : Y \rightarrow X$ is continuous
 - (4) all of the above

21. Let X be a non-empty set. Let T_1 and T_2 be two topologies on X such that T_1 is strictly contained in T_2 . If $I : (X, T_1) \rightarrow (X, T_2)$ is identity map, then:
- (1) both I and I^{-1} are continuous
 - (2) both I and I^{-1} are not continuous
 - (3) I is continuous but I^{-1} is not continuous
 - (4) I is not continuous but I^{-1} is continuous
22. The connected subset of real line with usual topology are --:
- (1) all intervals
 - (2) only bounded intervals
 - (3) only compact intervals
 - (4) only semi-infinite intervals
23. Topological space X is locally path connected space-
- (1) if X is locally connected at each $x \notin X$
 - (2) if X is locally connected at some $x \in X$
 - (3) if X is locally connected at each $x \in X$
 - (4) None of these
24. The topology on real line \mathbb{R} generated by left-open right closed intervals (a,b) is:
- (1) strictly coarser than usual topology
 - (2) strictly finer than usual topology
 - (3) not comparable with usual topology
 - (4) same as the usual topology
25. Which of the following is not first countable?
- (1) discrete space
 - (2) indiscrete space
 - (3) cofinite topological space on \mathbb{R}
 - (4) metric space

26. Let $X = \{a, b, c\}$ and $T_1 = \{\emptyset, \{a\}, \{b, c\}, X\}$

$X^* = \{x, y, z\}$ and $T_2 = \{\emptyset, \{x\}, \{y, z\}, X^*\}$

Then which of the following mapping from X to X^* are continuous?

(1) $f(a) = x, f(b) = y, f(c) = z$

(2) $g(a) = x, g(b) = y, g(c) = z$

(3) $h(a) = z, h(b) = x, h(c) = y$

(4) both (1) and (2)

27. A subspace of Hausdorff space is -

(1) Hausdorff space

(2) Discrete space

(3) Closed set

(4) None of these

28. Let X be a topological space satisfy first countability aniom if -

(1) the point $x \in \bar{A}$, closure of A in X iff there is a sequence of points of A converging to x

(2) The point $x \in \bar{A}$, closure of A in X iff there is a sequence of point of A diverging to x

(3) The point $x \in \bar{A}$, closure of A in X iff there is a sequence of point of A converging to zero

(4) None of these

29. Let X be non-empty compact Hausdorff space if every point of X is limit point of X , then:

(1) X is uncountable

(2) X is countable

(3) X is disjoint

(4) none of these

30. Let T_1 and T_2 be topological space. Under which condition a function $f : T_1 \rightarrow T_2$ is said to continuous?
- (1) iff pre-images of open sets are open
 - (2) iff pre images of every member of a base of T_2 is an open set in T_1
 - (3) both (1) and (2)
 - (4) iff pre-images of closed sets are not closed
31. Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be continuous function and let S be non-empty proper subset of \mathbb{R} . Which one of following statements is always true? (Here \bar{A} denote closure of A and A° denote interior of A)
- (1) $f(S)^\circ \subseteq f(S^\circ)$
 - (2) $f(\bar{S}) \subseteq \overline{f(S)}$
 - (3) $f(\bar{S}) \supseteq \overline{f(S)}$
 - (4) $f(S)^\circ \supseteq f(S^\circ)$
32. Let $T_1 = \{G \subseteq \mathbb{R} : G \text{ is finite or } \mathbb{R}/G \text{ is finite}\}$ and $T_2 = \{G \subseteq \mathbb{R} : G \text{ is countable or } \mathbb{R}/G \text{ is countable}\}$ then -
- (1) neither T_1 or T_2 is topology on \mathbb{R}
 - (2) T_1 is topology on \mathbb{R} but T_2 is not topology on \mathbb{R}
 - (3) T_2 is topology on \mathbb{R} but T_1 is not topology on \mathbb{R}
 - (4) Both T_1 and T_2 are topologies on \mathbb{R}
33. Let (X, T) be topological space. Every component of (X, T) is -
- (1) open
 - (2) closed
 - (3) both (1) and (2)
 - (4) none of these

34. Which of the following space is T_0 -space, T_1 -space and T_2 -space?
- (1) discrete space
 - (2) indiscrete space
 - (3) co-finite topological space
 - (4) both (1) and (2)
35. A finite space with cofinite topology is-
- (1) separable
 - (2) first-countable
 - (3) second-countable
 - (4) All of above
36. A sub-basis T for topology X is collection of subsets of X -
- (1) whose union equals X
 - (2) whose union is subset of X
 - (3) whose union is superset of X
 - (4) none of these
37. Every closed interval of real line R is -
- (1) uncountable
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38. Which of the following is not true?
- (1) if $A \subseteq B$ and $A^0 \subseteq B^0$
 - (2) every limit point is an adherent point
 - (3) $(A \cap B)^0 = A^0 \cap B^0$
 - (4) $(A \cup B)^0 \subseteq A^0 \cup B^0$

39. If Y is subspace of X . If A is closed in Y and Y is closed in X , then-

- (1) A is semi-closed in X
- (2) A is open in X
- (3) A is closed in X
- (4) none of these

40. If T_1 and T_2 are two topologies on non-empty set X , then which of the following is a topological space-

- (1) $T_1 \cup T_2$
- (2) $T_1 \cap T_2$
- (3) T_1 / T_2
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41. Which of the following statement is true about lower limit topology on \mathbb{R} ?

- (1) it is first countable
- (2) it is not separable
- (3) it is second countable
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42. If X is topological space, then-

- (1) each path component of X lies in component of X
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43. Let $X = \{a, b, c\}$ and $T = \{\phi, \{a\}, \{b, c\}, X\}$ which of the following is true?
- (1) $d(\{A\}) = \{B\}$
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44. Let (X, T) is given topological space, $A \subset X$, then closure of A-
- (1) is the intersection of all closed sets containing A
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 let $T_1 = \{\phi, X, \{\alpha\}, \{\alpha, \beta\}\}$ and
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 then -
- (1) both $T_1 \cap T_2$ and $T_1 \cup T_2$ are topologies
 - (2) neither $T_1 \cap T_2$ nor $T_1 \cup T_2$ is topology
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47. Let E be connected subset of \mathbb{R} with atleast two elements. Then number of elements in E is-
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1. Which of the following statement is true about lower limit topology on \mathbb{R} ?
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- Q : Every first - countable is second - countable
- R : Every T_0 -space is T_1 -space
- S : Every second-countable is first-countable
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and T_2 is discrete topology

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(3) T_2 is finer than T_1

(4) T_1 is coarser than T_2

22. A topological space X is compact if open covering of X contains-

- (1) finite subcollection that covers X
- (2) infinite subcollection that covers X
- (3) finite subcollection that does not cover X
- (4) none of these

23. Consider \mathbb{R}^2 with usual topology. Let

$$S = \{(x, y) \in \mathbb{R}^2 : x \text{ is an integer}\}$$

Then S is :

- (1) open but not closed
- (2) both open and closed
- (3) neither open nor closed
- (4) closed but not open

24. Suppose (X, T) is topological space. Let $\{S_n\}_{n \geq 1}$ be sequence of subsets of X .

Then-

- (1) $(S_1 \cup S_2)^0 = S_1^0 \cup S_2^0$
- (2) $(\bigcup_n S_n)^0 = \bigcup_n S_n^0$
- (3) $\overline{\bigcup_n S_n} = \bigcup_n \overline{S_n}$
- (4) $\overline{S_1 \cup S_2} = \overline{S_1} \cup \overline{S_2}$

25. A subspace of first countable space is-

- (1) first countable
- (2) not first-countable
- (3) second - countable
- (4) none of these

26. Let X and Y be topological spaces. A map $f : X \rightarrow Y$ is closed map if :
- (1) for every closed set U of X , the set $f(U)$ is closed in Y
 - (2) for every open set U of X , the set $f(U)$ is closed in Y
 - (3) for every closed set U of X , the set $f(U)$ is open in Y
 - (4) none of these
27. Let β and β' be basis for topologies T and T' respectively on X . Then T' is finer than T is equivalent to -
- (1) for each $x \in X$ and each basis element $B \in \beta$ containing x , there is basis element $B' \in \beta'$ such that $x \in B' \subset B$
 - (2) for some $x \in X$ and each basis element $B \in \beta$ containing x , there is a basis element $B' \in \beta'$ such that $x \in B' \subset B$
 - (3) for $x \in X$ and basis element $B \in \beta$ containing x , there is basis element $B' \in \beta'$ such that $x \in B' \subset B$
 - (4) none of these
28. A collection G of subsets of topological space satisfies finite intersection condition if for every finite subcollection $\{C_1, C_2, \dots, C_n\}$ of G , the intersection -
- (1) is null set
 - (2) is not null set
 - (3) is set G
 - (4) none of these
29. The product of two Hausdorff space is-
- (1) Hausdorff space
 - (2) discrete space
 - (3) closed set
 - (4) none of these

30. Let X and Y be topological spaces. Function f is homomorphism if :
- (1) function $f : X \rightarrow Y$ is one to one function
 - (2) function f is continuous
 - (3) inverse function $f^{-1} : Y \rightarrow X$ is continuous
 - (4) all of the above
31. Let X be a non-empty set. Let T_1 and T_2 be two topologies on X such that T_1 is strictly contained in T_2 . If $I : (X, T_1) \rightarrow (X, T_2)$ is identity map, then:
- (1) both I and I^{-1} are continuous
 - (2) both I and I^{-1} are not continuous
 - (3) I is continuous but I^{-1} is not continuous
 - (4) I is not continuous but I^{-1} is continuous
32. The connected subset of real line with usual topology are --:
- (1) all intervals
 - (2) only bounded intervals
 - (3) only compact intervals
 - (4) only semi-infinite intervals
33. Topological space X is locally path connected space-
- (1) if X is locally connected at each $x \in X$
 - (2) if X is locally connected at some $x \in X$
 - (3) if X is locally connected at each $x \in X$
 - (4) None of these
34. The topology on real line R generated by left-open right closed intervals (a,b) is:
- (1) strictly coarser than usual topology
 - (2) strictly finer than usual topology
 - (3) not comparable with usual topology
 - (4) same as the usual topology

35. Which of the following is not first countable?

- (1) discrete space
- (2) indiscrete space
- (3) cofinite topological space on \mathbb{R}
- (4) metric space

36. Let $X = \{a, b, c\}$ and $T_1 = \{\emptyset, \{a\}, \{b, c\}, X\}$

$X^* = \{x, y, z\}$ and $T_2 = \{\emptyset, \{x\}, \{y, z\}, X^*\}$

Then which of the following mapping from X to X^* are continuous?

- (1) $f(a) = x, f(b) = y, f(c) = z$
- (2) $g(a) = x, g(b) = y, g(c) = z$
- (3) $h(a) = z, h(b) = x, h(c) = y$
- (4) both (1) and (2)

37. A subspace of Hausdorff space is -

- (1) Hausdorff space
- (2) Discrete space
- (3) Closed set
- (4) None of these

38. Let X be a topological space satisfy first countability aniom if -

- (1) the point $x \in \bar{A}$, closure of A in X iff there is a sequence of points of A converging to x
- (2) The point $x \in \bar{A}$, closure of A in X iff there is a sequence of point of A diverging to x
- (3) The point $x \in \bar{A}$, closure of A in X iff there is a sequence of point of A converging to zero
- (4) None of these

39. Let X be non-empty compact Hausdorff space if every point of X is limit point of X , then:
- (1) X is uncountable
 - (2) X is countable
 - (3) X is disjoint
 - (4) none of these
40. Let T_1 and T_2 be topological space. Under which condition a function $f : T_1 \rightarrow T_2$ is said to continuous?
- (1) iff pre-images of open sets are open
 - (2) iff pre images of every member of a base of T_2 is an open set in T_1
 - (3) both (1) and (2)
 - (4) iff pre-images of closed sets are not closed
41. Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be continuous function and let S be non-empty proper subset of \mathbb{R} . Which one of following statements is always true? (Here \bar{A} denote closure of A and A^0 denote interior of A)
- (1) $f(S)^0 \subseteq f(S^0)$
 - (2) $f(\bar{S}) \subseteq \overline{f(S)}$
 - (3) $f(\bar{S}) \supseteq \overline{f(S)}$
 - (4) $f(S)^0 \supseteq f(S^0)$
42. Let $T_1 = \{G \subseteq \mathbb{R} : G \text{ is finite or } \mathbb{R}/G \text{ is finite}\}$ and $T_2 = \{G \subseteq \mathbb{R} : G \text{ is countable or } \mathbb{R}/G \text{ is countable}\}$ then -
- (1) neither T_1 or T_2 is topology on \mathbb{R}
 - (2) T_1 is topology on \mathbb{R} but T_2 is not topology on \mathbb{R}
 - (3) T_2 is topology on \mathbb{R} but T_1 is not topology on \mathbb{R}
 - (4) Both T_1 and T_2 are topologies on \mathbb{R}

43. Let (X, T) be topological space. Every component of (X, T) is -
- (1) open
 - (2) closed
 - (3) both (1) and (2)
 - (4) none of these
44. Which of the following space is T_0 -space, T_1 -space and T_2 -space?
- (1) discrete space
 - (2) indiscrete space
 - (3) co-finite topological space
 - (4) both (1) and (2)
45. A finite space with cofinite topology is-
- (1) separable
 - (2) first-countable
 - (3) second-countable
 - (4) All of above
46. A sub-basis T for topology X is collection of subsets of X -
- (1) whose union equals X
 - (2) whose union is subset of X
 - (3) whose union is superset of X
 - (4) none of these

47. Every closed interval of real line \mathbb{R} is -
- (1) uncountable
 - (2) countable
 - (3) disjoint
 - (4) none of these
48. Which of the following is not true?
- (1) if $A \subseteq B$ and $A^0 \subseteq B^0$
 - (2) every limit point is an adherent point
 - (3) $(A \cap B)^0 = A^0 \cap B^0$
 - (4) $(A \cup B)^0 \subseteq A^0 \cup B^0$
49. If Y is subspace of X . If A is closed in Y and Y is closed in X , then-
- (1) A is semi-closed in X
 - (2) A is open in X
 - (3) A is closed in X
 - (4) none of these
50. If T_1 and T_2 are two topologies on non-empty set X , then which of the following is a topological space-
- (1) $T_1 \cup T_2$
 - (2) $T_1 \cap T_2$
 - (3) T_1 / T_2
 - (4) none of these